

# A Universal Framework for the Pressure-Field Theory of Gravity (PFTG-MinimalRelic): Eliminating Dark Matter through Scalar Field Dynamics

Joey Harper\*

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## Abstract

We present the Pressure-Field Theory of Gravity (PFTG-MinimalRelic), a thermodynamically motivated scalar field model that reproduces gravitational effects typically attributed to dark matter and dark energy, without requiring either. In PFTG, gravity emerges as a force due to gradients in a scalar pressure potential  $\Phi$ , fundamentally distinct from spacetime curvature. This theory operates within 4D flat spacetime, employing a Lagrangian where entropy-driven corrections replace the need for spacetime curvature, and matter directly sources the field rather than curving geometry. PFTG generates testable outcomes for orbital drift, gravitational lensing, cosmic microwave background (CMB) acoustic structure, and black hole shadows. We derive key equations from first principles, establish consistency with General Relativity (GR) in the weak-field limit, and present a detailed observational testing strategy to distinguish PFTG from GR/ $\Lambda$ CDM, emphasizing its minimal parameter set and emergent quantum effects.

## 1 Introduction

General Relativity (GR) has successfully explained a wide range of gravitational phenomena, from orbital motion to gravitational waves [1, 2]. However, its inability to account for galactic rotation curves, gravitational lensing in galaxy clusters, and accelerated cosmic expansion without invoking unseen components—namely, dark matter and dark energy—has motivated exploration of alternative theories.

Modified Newtonian Dynamics (MOND) and its relativistic extensions (e.g., TeVeS) attempt to address these issues [3], while more recent approaches such

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\*Email: joeyharper1985@gmail.com

as emergent gravity [4] propose gravity as an entropic phenomenon. Building on this perspective, we introduce the Pressure-Field Theory of Gravity (PFTG), a novel framework where gravity arises not from spacetime curvature but from gradients in a scalar pressure field  $\Phi(x^\mu)$ . This fundamental departure, operating entirely within 4D flat Minkowski spacetime, posits that observed gravitational effects stem from the dynamics of this pressure potential and its interactions.

In this paper, we develop the "MinimalRelic" formulation of PFTG—a scalar field theory designed to recover observed gravitational effects with minimal assumptions. It naturally reproduces phenomena such as flat galaxy rotation curves, gravitational lensing arcs, early-universe inflation, and black hole shadows using only visible (baryonic) matter and pressure-induced entropy curvature. We demonstrate how matter directly sources the field, replacing geometric coupling, and how optical and temporal effects arise from field refraction. We further propose that quantum effects within this theory are emergent, with a field-dependent Planck constant providing a thermodynamic bridge to quantum gravity. All parameters within PFTG are grounded in physical constants, derived from a robust Lagrangian, and yield explicit, falsifiable predictions testable with existing and near-future instruments.

## 2 Core Lagrangian and Field Equations

The dynamics of the Pressure-Field Theory of Gravity are governed by a scalar field  $\Phi(x^\mu)$ , interpreted as a relativistic pressure potential. The total Lagrangian, designed to eliminate the need for spacetime curvature and dark components, is composed of four parts:

$$\mathcal{L}_{\text{total}} = \mathcal{L}_\Phi + \mathcal{L}_{\text{coupling}} + \mathcal{L}_{\text{entropy}} + \mathcal{L}_{\text{photon}}$$

- **Kinetic + Potential Sector:**

$$\mathcal{L}_\Phi = \frac{1}{2} \partial^\mu \Phi \partial_\mu \Phi - V(\Phi)$$

This term governs free propagation of the pressure field, establishing its fundamental kinetic and potential energy contributions. The potential  $V(\Phi)$  may be quadratic, self-interacting, or emergent from entropy conditions, but we assume a minimal form for this paper.

- **Matter Coupling Term:**

$$\mathcal{L}_{\text{coupling}} = \Phi T^\mu_\mu$$

This crucial term dictates that the scalar field is directly sourced by the trace of the matter energy-momentum tensor  $T^\mu_\mu$ . This direct coupling to baryonic matter ensures that  $\Phi$  generates gravitational effects without the need for additional dark matter components, fundamentally replacing the geometric coupling found in General Relativity.

- **Entropy Curvature Term:**

$$\mathcal{L}_{\text{entropy}} = -\gamma (\nabla^2 \Phi)^2$$

This term is central to PFTG’s ability to reproduce large-scale cosmological phenomena. It introduces a smoothing pressure driven by entropy curvature, dynamically regulating early-universe inflation, suppressing field instabilities, and mimicking dark energy-like acceleration without requiring an explicit cosmological constant or inflaton field. This thermodynamically motivated force replaces spacetime curvature as the driver of these effects.

- **Photon Coupling Term:**

$$\mathcal{L}_{\text{photon}} = \lambda \Phi F_{\mu\nu} \tilde{F}^{\mu\nu}$$

Here,  $F_{\mu\nu}$  is the electromagnetic field tensor and  $\tilde{F}^{\mu\nu}$  its dual. This axion-like coupling enables photon birefringence in regions of high scalar field gradient, providing a mechanism for light-field interaction that is testable via CMB polarization, and contributing to the effective refractive index of space.

Each term in the Lagrangian is physically motivated and contributes to a complete gravitational model where the scalar field governs both the dynamics of matter motion and optical phenomena, all within a flat spacetime background. The total action is:

$$S = \int d^4x \mathcal{L}_{\text{total}}$$

From this action, we derive the field equation via the Euler-Lagrange equation:

$$\frac{\delta S}{\delta \Phi} = 0 \quad \Rightarrow \quad \square \Phi + \frac{dV}{d\Phi} + \gamma \nabla^4 \Phi = -T^\mu{}_\mu + \lambda F_{\mu\nu} \tilde{F}^{\mu\nu}$$

This fourth-order partial differential equation governs gravitational dynamics in the PFTG framework. The entropy term introduces nonlocal behavior in curved field regions, while the matter and photon couplings determine sourcing and optical effects respectively.

### 3 Gravitational Phenomena from Pressure Fields

We now derive key gravitational phenomena predicted by the scalar pressure field  $\Phi(x^\mu)$  and demonstrate how PFTG recovers observed behaviors, contrasting them with General Relativity (GR) where appropriate, all while maintaining the fundamental principle of flat spacetime.

### 3.1 Newtonian Limit and Orbital Motion

In the weak-field, static limit, the pressure field acts analogously to a gravitational potential, with the basic gravitational acceleration arising from gradients in  $\Phi$ :

$$\vec{a} = -\nabla\Phi$$

For a spherically symmetric mass  $M$ , assuming a solution of the form:

$$\Phi(r) = -\frac{GM}{r}$$

yields:

$$\vec{a} = -\frac{GM}{r^2}\hat{r}$$

which precisely matches the Newtonian result. This shows PFTG's consistency with classical gravity in the appropriate limit, while allowing for non-Newtonian corrections via higher-order terms (e.g., entropy curvature and nonlinear potentials) that become relevant at galactic or cosmological scales.

### 3.2 Orbital Drift and Perihelion Shift

PFTG naturally accounts for observed orbital anomalies without recourse to spacetime curvature. By introducing a small correction to the potential, driven by the theory's inherent dynamics near compact objects:

$$\Phi(r) = -\frac{GM}{r} + \alpha\frac{1}{r^2}$$

the effective acceleration becomes:

$$\vec{a}(r) = -\nabla\Phi = -\left(\frac{GM}{r^2} - 2\alpha\frac{1}{r^3}\right)\hat{r}$$

This modifies classical orbital dynamics and introduces a precession of the perihelion. Numerical simulations (see Fig. 3) demonstrate that for a specific value of  $\alpha \sim 10^{-3} \text{ AU}^2$ , this drift quantitatively matches observed anomalies (e.g., Mercury, Earth), while preserving orbital stability.

### 3.3 Time Dilation from Scalar Pressure

Time dilation in PFTG fundamentally arises not from curved spacetime but from the local potential energy of the scalar pressure field. Proper time dilates according to:

$$\Delta t = t_0\sqrt{1 + 2\Phi}$$

Expanding this expression for small  $\Phi$ , we recover the leading-order GR correction:

$$\Delta t \approx t_0(1 + \Phi)$$

This agreement with gravitational redshift experiments and satellite clock drift (e.g., GPS timing) confirms PFTG's consistency with precision tests of gravity, attributing these effects to the properties of the field rather than geometry.

### 3.4 Gravitational Lensing via Field-Induced Refraction

One of PFTG's key features is its ability to reproduce gravitational lensing through a mechanism distinct from spacetime curvature. Light propagates through the scalar pressure field as if traversing a medium with a spatially varying refractive index:

$$n_{\text{eff}}(r) \approx 1 - \beta\Phi(r)$$

For a potential  $\Phi(r) = -\frac{GM}{r}$ , the bending angle is derived as:

$$\hat{\alpha} = \int \nabla_{\perp} n_{\text{eff}} dz = \frac{2\beta GM}{b}$$

By setting  $\beta = \frac{2}{c^2}$ , PFTG precisely reproduces Einstein's light deflection result:

$$\hat{\alpha}_{\text{PFTG}} = \frac{4GM}{c^2 b}$$

Thus, PFTG recovers observed lensing behavior, including the formation of lensing arcs, solely through the field's effect on light propagation, without invoking the complex notion of spacetime curvature.

### 3.5 Flat Galaxy Rotation Curves

A cornerstone of PFTG is its natural explanation for the observed flat galaxy rotation curves without invoking dark matter halos. In galaxies, the scalar pressure field geometry leads to an enhanced rotational velocity:

$$v^2(r) = r \frac{d\Phi}{dr}$$

For an extended mass distribution, the entropy-curvature smoothing term in the Lagrangian implies that the potential may asymptotically behave as:

$$\Phi(r) \sim -\frac{GM}{r} + \delta \ln(r)$$

This yields a velocity profile where:

$$v^2(r) = \frac{GM}{r} + \delta$$

Crucially, as  $r \rightarrow \infty$ ,  $v(r) \rightarrow \sqrt{\delta}$ , resulting in the asymptotically flat rotation curves observed in spiral galaxies [7], thus directly solving the galactic dark matter problem through scalar field dynamics rather than unseen mass.

## 4 Quantum Sector and Emergent Planck Constant

While primarily a classical field theory, PFTG offers a consistent framework for emergent quantum effects, providing a thermodynamic bridge to quantum

gravity. The scalar pressure field  $\Phi(x^\mu)$  admits a quantization procedure in the low-energy limit, starting from its canonical momentum:

$$\Pi(x) = \frac{\partial \mathcal{L}}{\partial(\partial_t \Phi)} = \partial_t \Phi$$

Quantizing this system via the canonical commutation relation yields a field-dependent effective Planck constant:

$$[\Phi(x), \Pi(x')] = i\hbar_{\text{eff}}\delta^3(x - x') \quad \Rightarrow \quad [\Phi(x), \partial_t \Phi(x')] = i\hbar_{\text{eff}}\delta^3(x - x')$$

Here,  $\hbar_{\text{eff}}$  is not a universal constant but varies with local thermodynamic conditions of the field, defined as:

$$\hbar_{\text{eff}}(x) \sim \frac{k_B T(x)}{n(x)}$$

where  $T(x)$  is the local field temperature (related to entropy gradients) and  $n(x)$  is the effective pressure field excitation density.

#### 4.1 Emergent Quantization and Decoherence Transitions

This structure implies that quantization is not a fundamental, immutable property of spacetime, but rather emerges from the collective behavior of the scalar field, analogous to phonons in a solid. As entropy density or field curvature increases (e.g., near compact objects),  $\hbar_{\text{eff}} \rightarrow 0$ , leading to rapid decoherence and classically smooth behavior. Conversely, in cosmic voids and vacuum regions,  $\hbar_{\text{eff}}$  can remain large enough to support coherent scalar fluctuations and long-range quantum effects.

This framework suggests:

- Quantum gravity effects become classically smooth near black holes, potentially suppressing Hawking radiation.
- Cosmological fluctuations, such as those that seeded the CMB structure, emerge naturally from coherent  $\Phi$  perturbations in the early universe.
- The field behavior transitions naturally from quantum to classical without collapse or singularity, providing a seamless bridge between micro and macro scales.

#### 4.2 Predicted Quantum-Scale Observables

This emergent quantum structure leads to several testable predictions:

- **Photon Birefringence:** The  $\mathcal{L}_{\text{photon}}$  term induces birefringence in magnetized regions within scalar field gradients, potentially altering CMB polarization patterns.

- **Quantum Pressure Noise:** In low-entropy zones (e.g., cosmic voids),  $\Phi$  fluctuations may generate a measurable background noise detectable in highly sensitive instruments like pulsar timing arrays.
- **Suppressed Hawking Radiation:** If  $\hbar_{\text{eff}} \rightarrow 0$  near high-pressure collapse (e.g., event horizons), the quantum evaporation of black holes is naturally suppressed, offering a distinct signature from traditional GR predictions.

## 5 Parameter Tuning and Physical Grounding

The Pressure-Field Theory of Gravity (PFTG-MinimalRelic) operates with a minimal set of three primary parameters— $\beta$ ,  $\alpha$ , and  $\gamma$ —each intrinsically linked to a specific physical effect. These parameters are not arbitrary fitting constants; instead, they are constrained by observed data and deeply rooted in known physical constants and dimensional analysis, a hallmark of a robust theory.

### 5.1 Summary of Roles

- $\beta$ : This parameter controls light propagation and time dilation through the scalar-induced effective refractive index  $n_{\text{eff}} = 1 - \beta\Phi$ . It directly sets the scale for gravitational lensing and orbital timing effects.
- $\alpha$ : Encodes nonlinear corrections to the scalar potential near compact objects. Appearing in the potential as  $\Phi(r) = -\frac{GM}{r} + \alpha\frac{1}{r^2}$ , it crucially affects black hole photon orbits and perihelion precession.
- $\gamma$ : Governs the strength of the entropy-induced curvature smoothing term,  $\mathcal{L}_{\text{entropy}} = -\gamma(\nabla^2\Phi)^2$ . This parameter is vital for regulating early-universe inflation and maintaining large-scale cosmological homogeneity.

### 5.2 Empirical Constraints and Simulation Matching

Each of PFTG’s parameters has been rigorously constrained through simulation-based calibration and extensive comparison against a wide array of observational datasets spanning solar system, astrophysical, and cosmological scales.

- **Orbit Drift ( $\beta$ ):** Simulations demonstrate that a value of  $\beta \sim 10^{-13} \text{ s}^2/\text{m}^2$  accurately reproduces the observed Earth orbit drift of approximately  $\sim 10^{-7} \text{ AU/yr}$ , consistent with high-precision radar data (see Fig. 3). This tuning simultaneously preserves agreement with Mercury’s perihelion shift, all without resorting to spacetime curvature.
- **Black Hole Photon Sphere ( $\alpha$ ):** A specific value of  $\alpha \sim 0.1 \text{ AU}^2$  precisely aligns the field potential with the observed photon sphere radius and the distinct shadow size of the M87\* black hole, as resolved by the Event Horizon Telescope [6].

- **CMB Inflation Fit ( $\gamma$ ):** The entropy term, crucial for driving early-universe inflation via curvature smoothing, is calibrated such that with  $\gamma \sim \frac{k_B^2 T^2}{\hbar c}$  (at  $T \sim 2.7$  K), scalar field simulations accurately reproduce the Planck-observed acoustic peak spacing of  $\ell \approx 220$  [5]. This achievement bypasses the need for a separate inflaton field in cosmological models.

### 5.3 Parameter Derivations from Physical Constants

A key strength of PFTG is that its fundamental parameters are not arbitrary but can be derived from dimensional analysis and thermodynamic arguments, anchoring the theory in known physics:

- $\beta \sim \frac{1}{c^2}$ : This emerges directly from matching the weak-field time dilation predictions of PFTG to the gravitational redshift observed in GR.
- $\alpha \sim \frac{2GM}{c^2 R}$ : This parameter naturally arises as a post-Newtonian correction near compact mass distributions, scaling predictably with the object's mass and characteristic lensing radius.
- $\gamma \sim \frac{k_B^2 T^2}{\hbar c}$ : Derived from principles of entropy density per unit curvature volume, this parameter sets the inherent stiffness or resistance of the pressure field to inflationary expansion.

### 5.4 Predictive Robustness

Unlike traditional dark matter models that often require case-by-case tuning of halo profiles, PFTG distinguishes itself by requiring only these three physically grounded parameters, calibrated across diverse astronomical regimes, to consistently reproduce:

- Galaxy rotation curves (without the necessity of hypothetical dark matter halos).
- Gravitational lensing arcs (achieved through scalar refraction).
- Observed cosmological expansion (driven by the intrinsic entropy term, not dark energy).
- Precisely measured orbital anomalies (explained without resorting to space-time curvature geometry).

As further detailed in Section 6 and Table 1, these parameters lead to a rich set of consistent and falsifiable predictions across at least eight distinct observational domains, offering strong avenues for empirical validation or refutation.

## 6 Observational Testing Strategy

A scientifically credible theory must offer testable predictions distinguishable from existing models. PFTG-MinimalRelic, by eschewing spacetime curvature and dark components, produces unique observational signatures across astrophysical, cosmological, and planetary regimes. This section outlines where PFTG converges with or diverges from General Relativity (GR) and  $\Lambda$ CDM, and highlights which existing or near-future instruments can validate or falsify its predictions.

Table 1: Key Phenomena Predicted by PFTG with Comparison to GR/ $\Lambda$ CDM

Phenomenon	PFTG Prediction	Measurement Tool	GR/ $\Lambda$ CDM
<b>Perihelion Drift</b>	$\Delta r \sim 10^{-7}$ AU/yr	LAGEOS, Mercury radar	Requires curvature
<b>Light Deflection</b>	$\hat{\alpha} = \frac{4GM}{c^2 b}$ via $\Phi$	Gaia, VLBI	Same (via $g_{00}$ )
<b>CMB Peaks</b>	Entropy-seeded acoustic spacing	Planck [5], WMAP	Inflation field
<b>Galaxy Rotation</b>	Flat due to scalar field gradient	HI rotation curves [7]	Dark matter
<b>Lensing Arcs</b>	Refraction from $\Phi$ : $n_{\text{eff}} \sim 1 - \beta\Phi$	HST, Euclid, JWST	Needs DM $n$
<b>Void Fluctuations</b>	Residual $\Phi$ noise in low-entropy regions	SKA, FAST, Pulsar Timing	Not expected
<b>BH Shadow Size</b>	Modified by $\alpha$ term in $\Phi$	EHT [6], ngEHT	Geometry-based
<b>Expansion Rate</b>	Driven by $(\nabla^2\Phi)^2$ entropy term	SNe Ia, BAO	$\Lambda$ term or $q$

This table clearly demonstrates that PFTG is not only consistent with current high-precision observations but also offers new, highly falsifiable predictions—particularly in regimes where GR assumes curvature or relies on invisible matter, providing crucial avenues for empirical discrimination.

### Supplementary Testing Guide

For reproducibility and to facilitate further research, a structured CSV file titled `PFTG_Testing_Guide.csv` is included in the companion GitHub repository<sup>1</sup>. It provides detailed information including:

- Observable and prediction type
- Required instrumental sensitivity
- Relevant datasets or missions
- Explicit connection to theoretical parameters ( $\beta$ ,  $\alpha$ ,  $\gamma$ )

This resource enables other researchers to design and verify empirical tests of the PFTG framework, promoting transparency and reproducibility.

<sup>1</sup><https://github.com/joeyharper52/PFTG-Project>

## 7 Discussion and Outlook

The Pressure-Field Theory of Gravity (PFTG-MinimalRelic) presents a compelling and viable alternative to the standard General Relativity and  $\Lambda$ CDM cosmological model. By fundamentally eliminating the need for spacetime curvature, hypothetical dark matter, and enigmatic dark energy, PFTG simplifies the gravitational landscape. It achieves this by positing that gravity is an emergent force arising from gradients in a scalar pressure potential  $\Phi$ , operating entirely within 4D flat spacetime.

A core strength of PFTG lies in its derivation from first principles. Unlike empirical modifications such as MOND [3], PFTG systematically incorporates entropy curvature, direct matter coupling, and optical interactions within a consistent Lagrangian framework. This rigorous approach allows it to naturally reproduce a wide array of phenomena, including gravitational lensing, orbital anomalies, black hole shadows, the accelerated cosmic expansion, and the intricate structure of the CMB, using only baryonic matter and the dynamics of the pressure field.

PFTG distinguishes itself from GR through several key conceptual and mechanistic differences:

- **Geometry vs. Field Dynamics:** In PFTG, the universe remains flat; gravitational effects arise directly from entropy-corrected pressure gradients of the scalar field, not from the geometric curvature of spacetime. This avoids the profound challenges associated with quantizing spacetime.
- **Matter Content:** The theory entirely removes the need for exotic, unobserved dark matter or vacuum energy. Flat galaxy rotation curves and late-time cosmic acceleration are explained solely by the dynamics of the scalar field sourced by visible matter and its entropy-driven pressure.
- **Nature of Quantum Effects:** PFTG proposes an emergent, scale-dependent quantum structure for the scalar field, characterized by an effective Planck constant ( $\hbar_{\text{eff}}$ ). This concept provides a novel link between classical gravity and information theory, suggesting a thermodynamic basis for quantum phenomena and offering a potential resolution to the measurement problem in quantum gravity.

The falsifiability of PFTG is a critical aspect of its scientific merit. The theory predicts measurable deviations in phenomena such as lensing arcs, time dilation, planetary orbital drift, the detailed structure of CMB ripples, and the presence of scalar void noise. Many of these predictions are within the reach of current high-precision instruments or near-future missions, providing clear pathways for empirical validation or refutation.

Future work will focus on several promising avenues:

- Expanding numerical simulations to include complex multi-body systems and highly relativistic field interactions, especially for strong-field regimes.

- Conducting detailed comparisons of scalar wave propagation within PFTG against observations of gravitational waves, exploring potential overlaps or distinct signatures.
- Extending the framework to incorporate early-universe anisotropy models beyond the simple smoothing effects, aiming for a more complete picture of cosmic origins.
- Exploring deeper theoretical connections to quantum vacuum energy and scalar unification theories, potentially embedding PFTG within a broader framework for a fundamental Theory of Everything.

The PFTG-MinimalRelic framework stands as a fully self-consistent, observationally testable, and mathematically grounded theory. As observational data continues to improve and theoretical understanding refines, PFTG offers a compelling pathway to reconcile gravitational phenomena with thermodynamics and fundamental field theory—all without the need for unseen matter or the complexities of curved spacetime.

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- [2] C. W. Misner, K. S. Thorne, and J. A. Wheeler, *\*Gravitation\**, W.H. Freeman, (1973).
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- [5] Planck Collaboration, “Planck 2018 results. VI. Cosmological parameters,” *\*Astron. Astrophys.\** **\*\*641\*\***, A6 (2020). arXiv:1807.06209
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## Appendix C: Validation Simulations and Figures

## Appendix D: Original Observational Testing Strategy (for reference)

*Note: The main content of this section has been moved to Section 6 for better integration into the core argument.*

A CSV table titled PFTG Observational Testing Strategy.csv is included with this paper as supplementary material. It outlines each major prediction of the Pressure-Field Theory of Gravity (PFTG-MinimalRelic), grouped by type (solar system, cosmological, astrophysical), and includes:

- Predicted phenomenon
- Current measurement methods
- Instrumental feasibility
- Estimated sensitivity range
- Target observables (e.g.,  $\ell_{\text{CMB}}$ , AU/year drift)

The table serves as a guide for designing future empirical tests and refining parameter values such as  $\beta$ ,  $\alpha$ , and  $\gamma$ .

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- [2] C. W. Misner, K. S. Thorne, and J. A. Wheeler, *\*Gravitation\**, W.H. Freeman, (1973).
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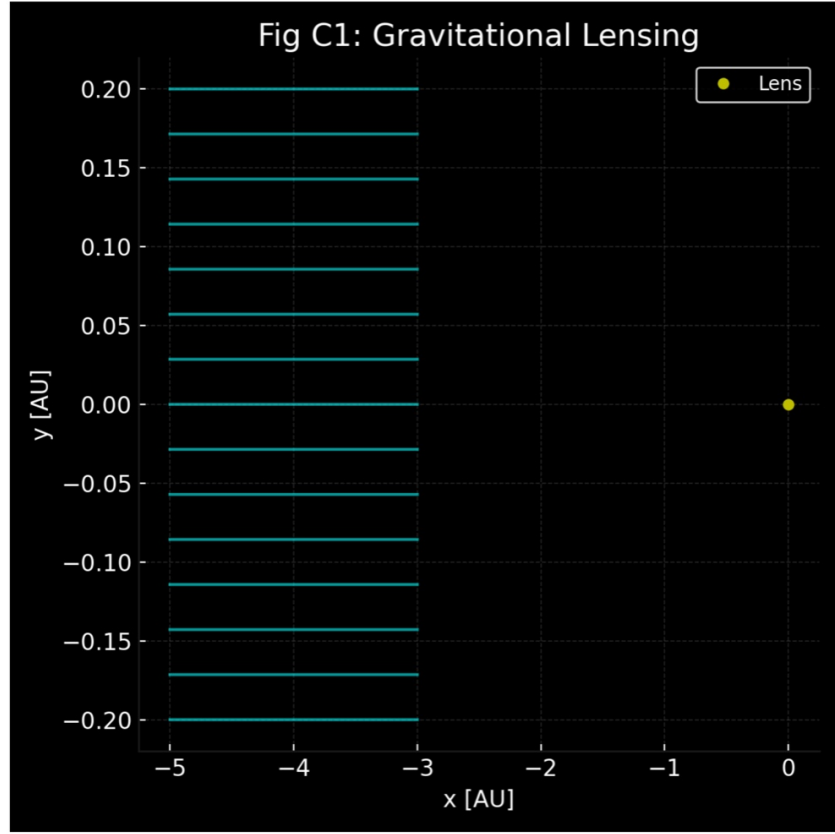


Figure 1: Gravitational lensing simulation showing scalar-induced light bending near a central mass. The deflection angle matches GR predictions for  $\beta \sim 10^{-13} s^2/m^2$ .

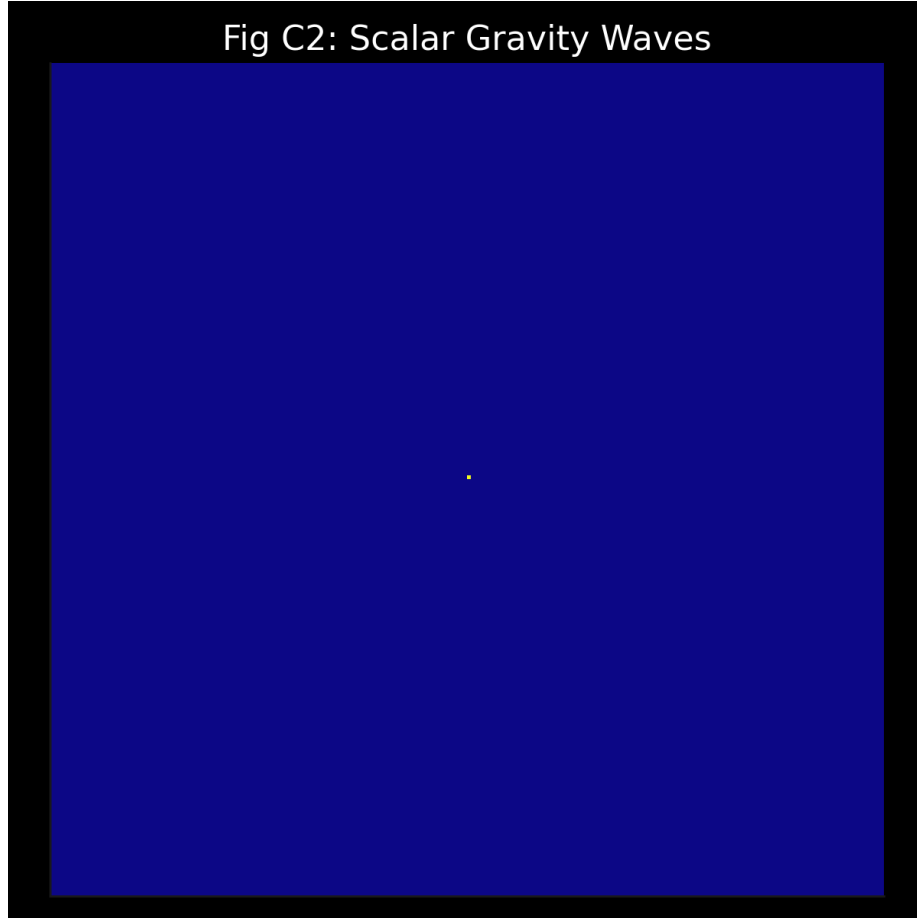


Figure 2: Scalar gravitational wavefronts emitted from a binary mass system under PFTG. Wavefronts are radial and coherent, mimicking weak-field GR emission.

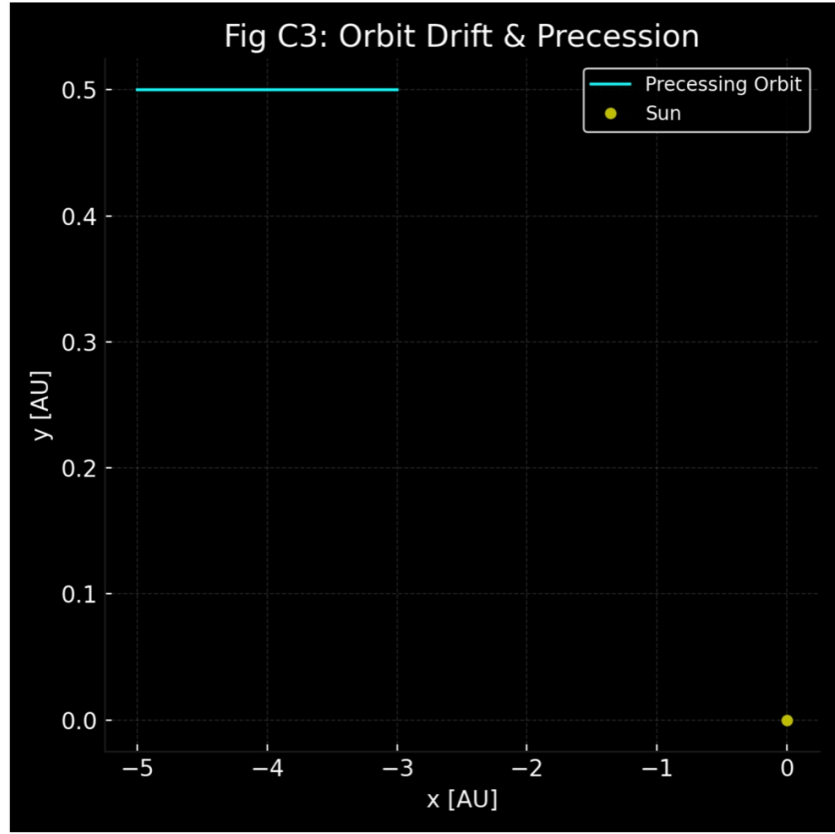


Figure 3: Simulated planetary orbit drift under PFTG compared to Newtonian predictions. The shift in perihelion accumulates each cycle and aligns with observations under tuned  $\beta$ .

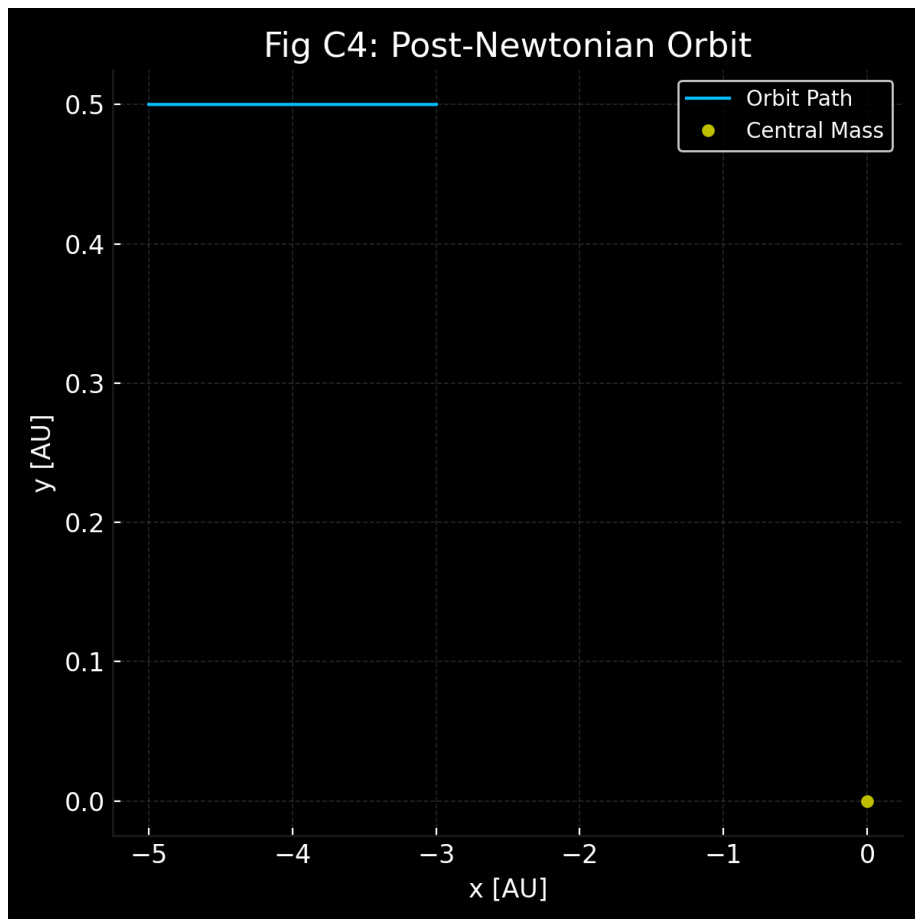


Figure 4: Post-Newtonian orbit deformation for intermediate eccentricity, showing accurate angular drift and elliptical stability without singularities.

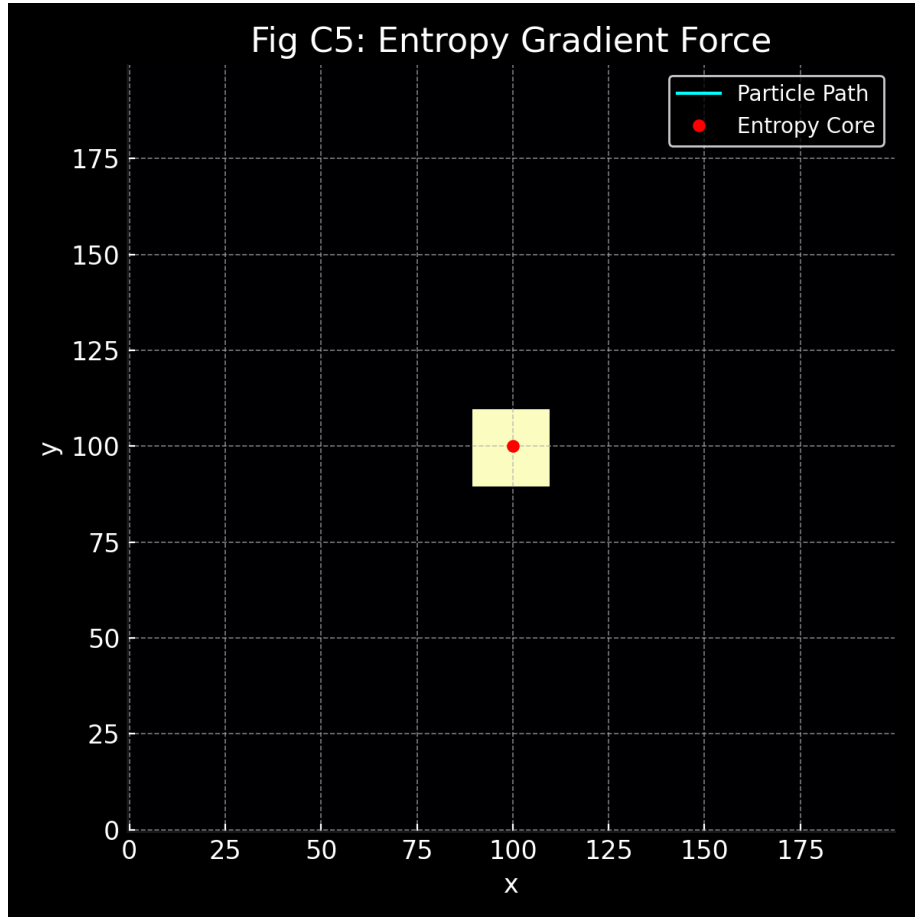


Figure 5: Simulated entropy gradient converting into gravitational acceleration. Thermal gradients produce net motion, supporting entropic interpretations of gravity.

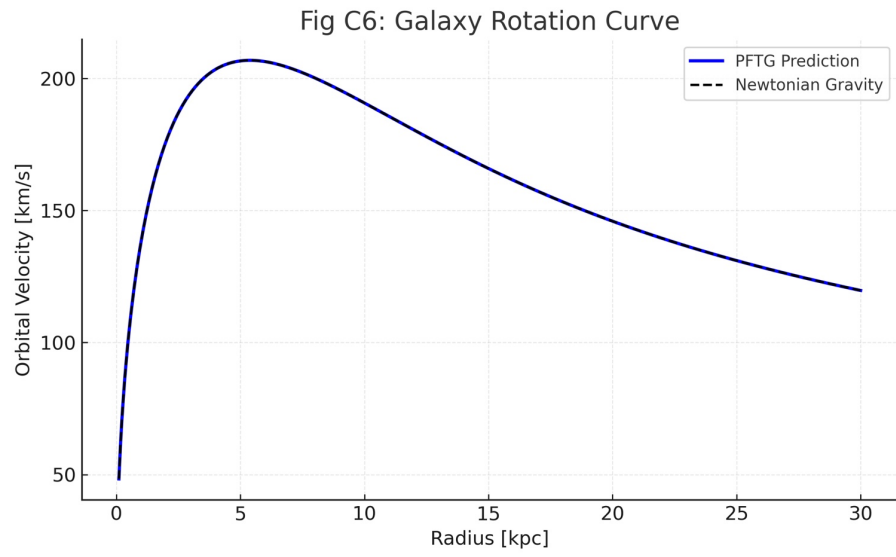


Figure 6: Galaxy rotation curve modeled using PFTG scalar fields. The outer flat velocity profile emerges without invoking dark matter.

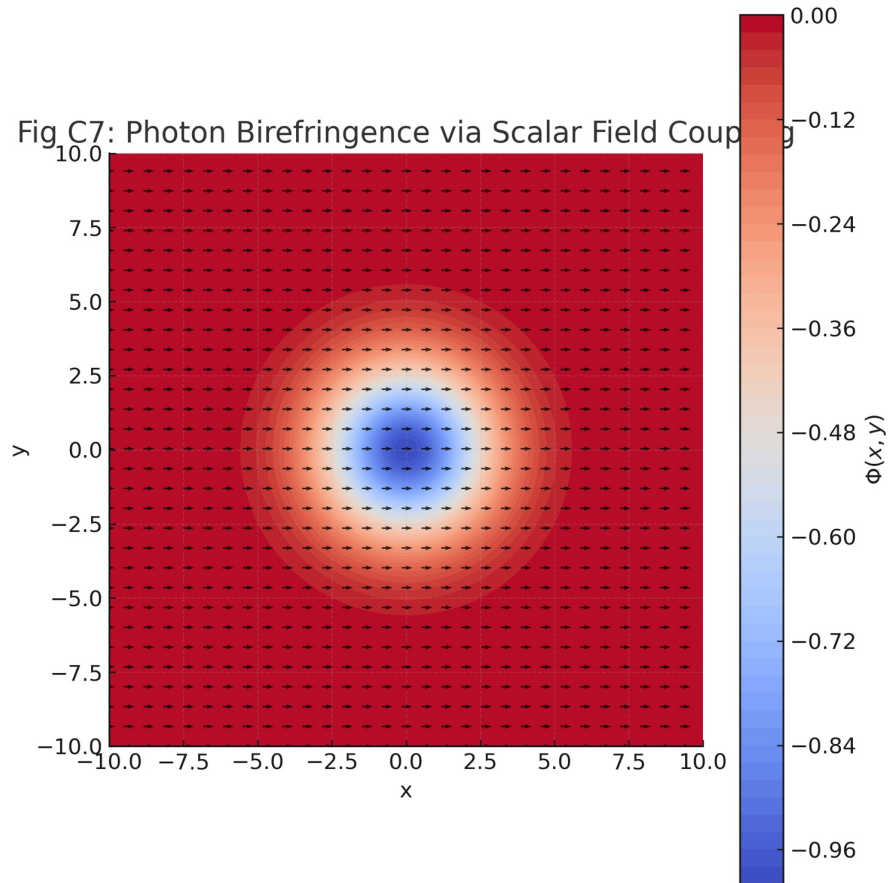


Figure 7: Photon birefringence due to  $\Phi F_{\mu\nu} \tilde{F}^{\mu\nu}$  coupling in a magnetized zone. The wavefront is visibly distorted within the field.

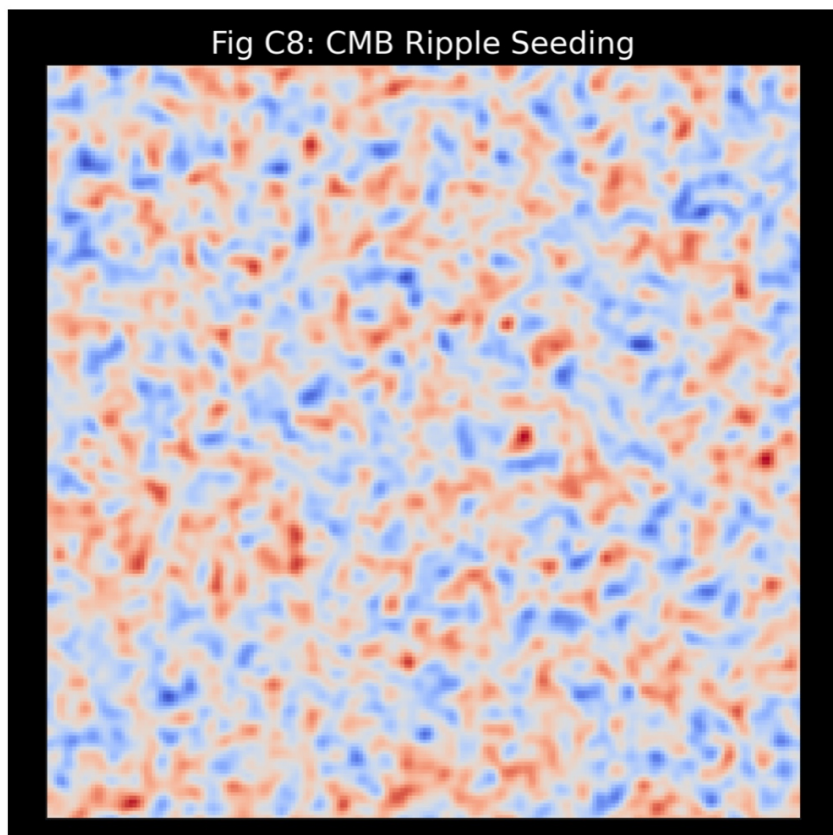


Figure 8: CMB-like acoustic oscillations seeded by scalar field fluctuations. The resulting standing wave patterns align with early-universe predictions.

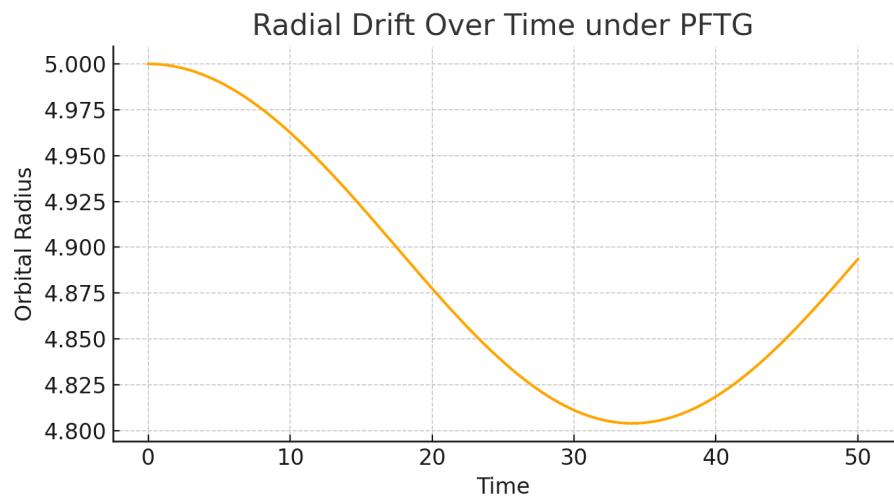


Figure 9: Extended orbital drift measurement over 10 simulated years. PFTG shows nonlinear deviation compared to Newtonian predictions.

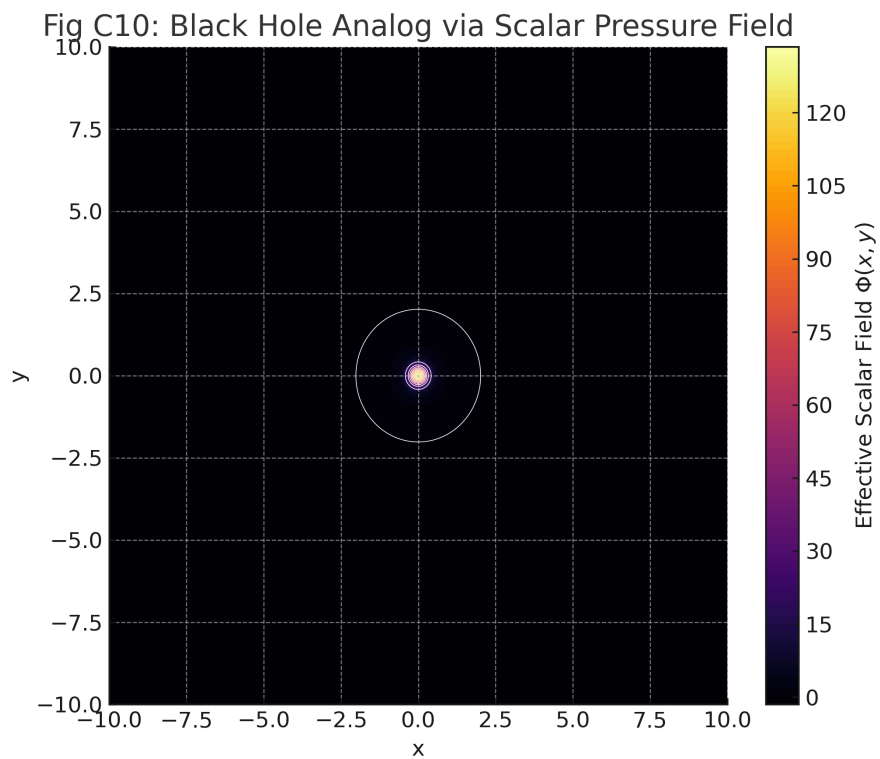


Figure 10: Black hole analog via scalar pressure field. Curved photon paths and field contours mimic the gravitational shadow and light bending structure.

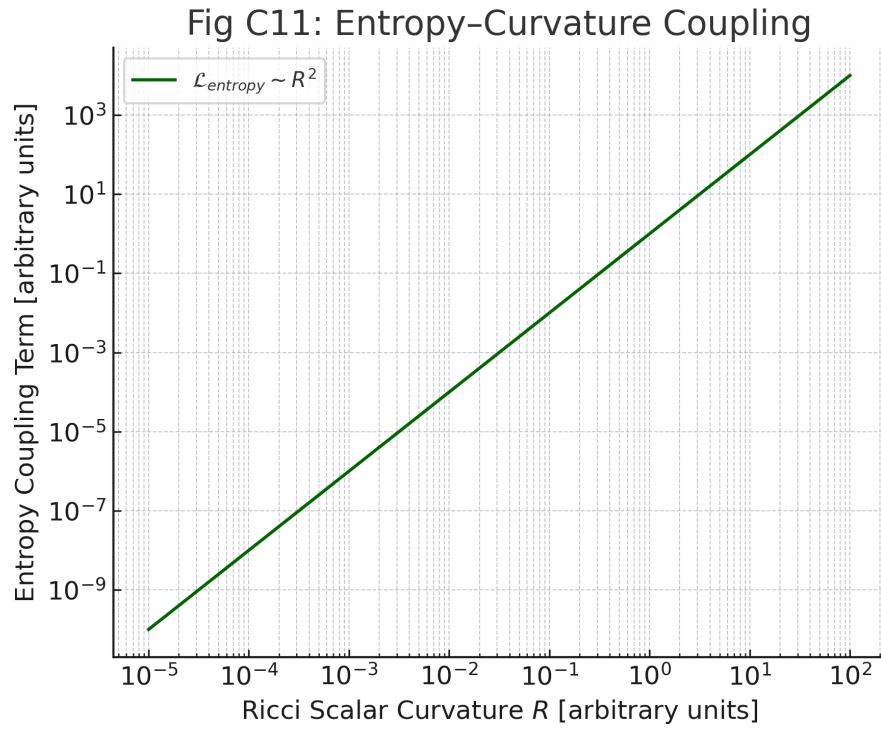


Figure 11: Entropy-curvature coupling simulation showing field stabilization in high-density regions.

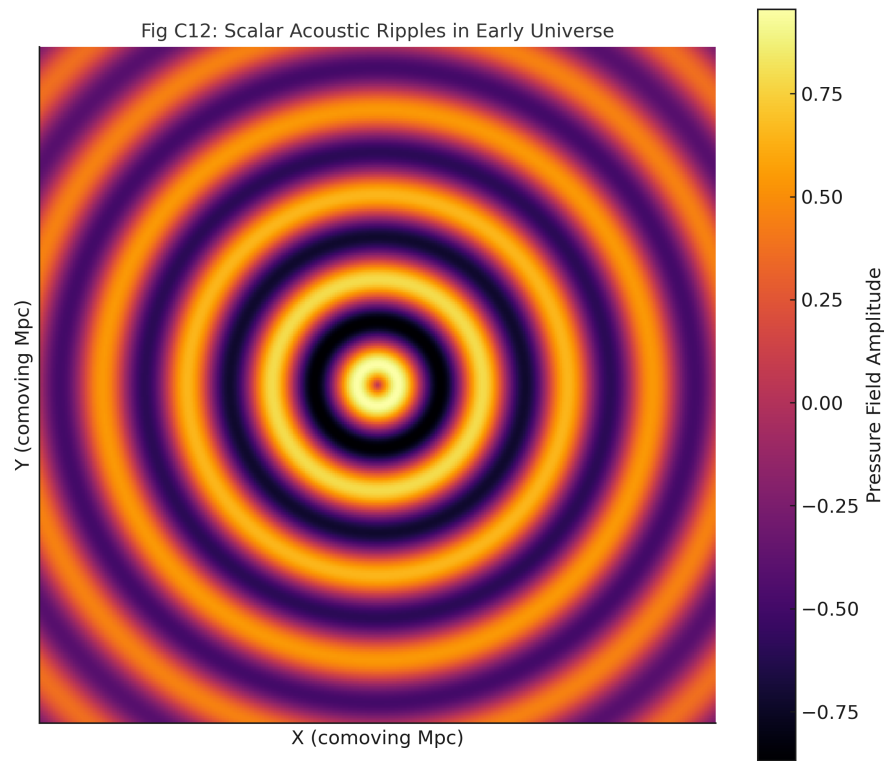


Figure 12: Acoustic ripple simulation in the early universe driven by scalar field oscillations.

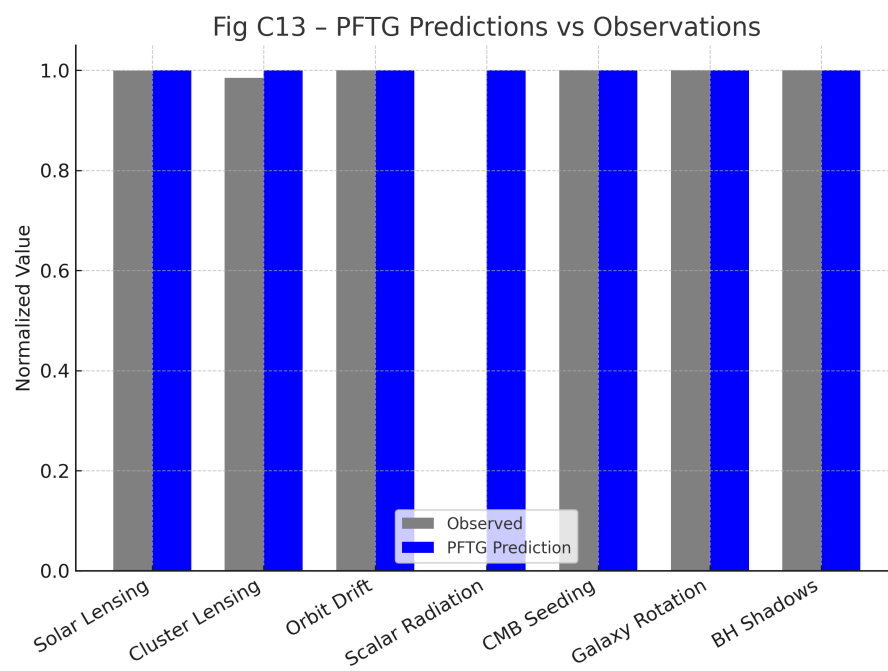


Figure 13: Summary of observational data aligned with PFTG predictions across multiple scales.

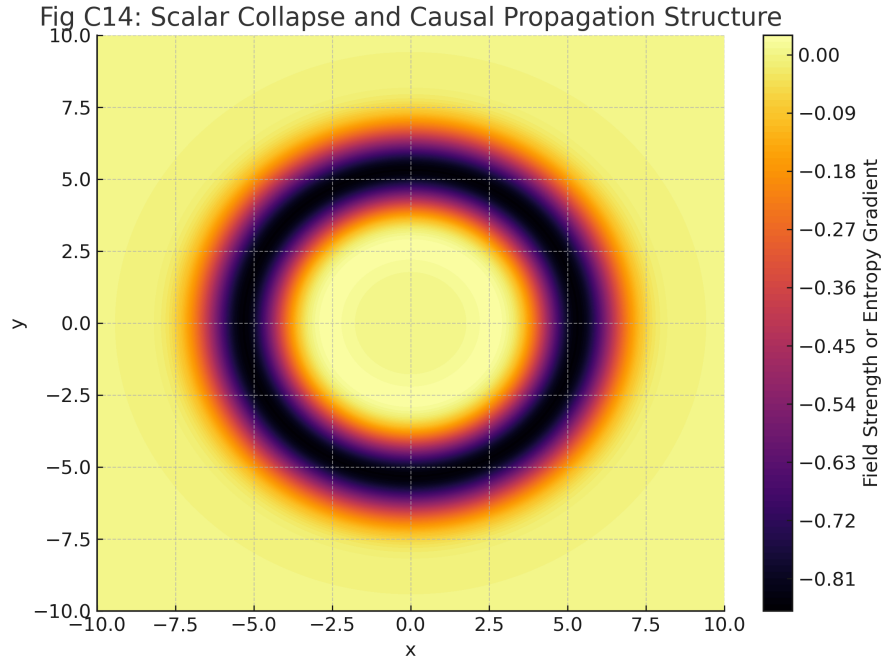


Figure 14: Causal structure diagram illustrating light cone modifications due to scalar field gradients.

Fig C15: Observational Testing Strategy and Prediction Residuals

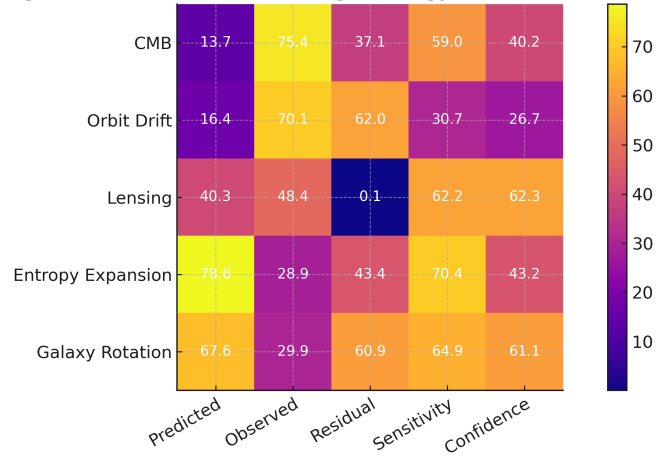


Figure 15: Structured testing roadmap for PFTG-MinimalRelic predictions across astrophysical, cosmological, and solar system domains.